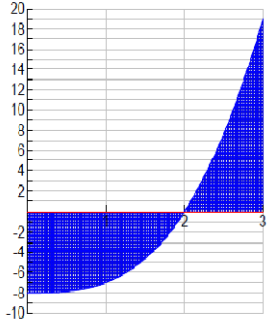
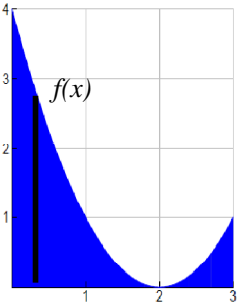
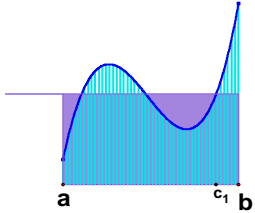
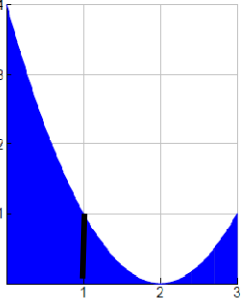
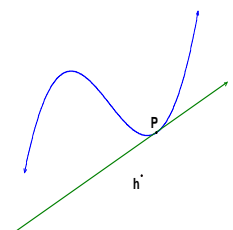
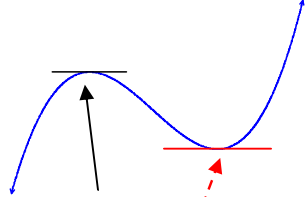
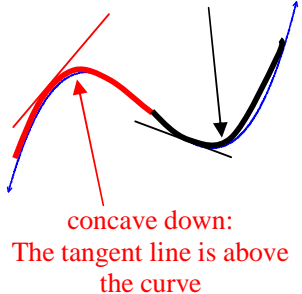
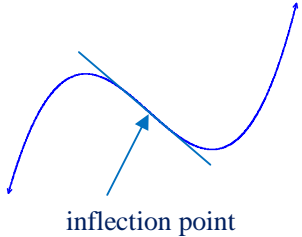
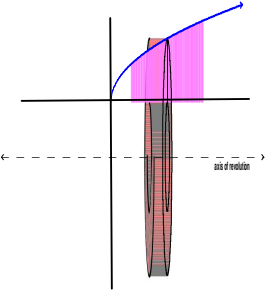
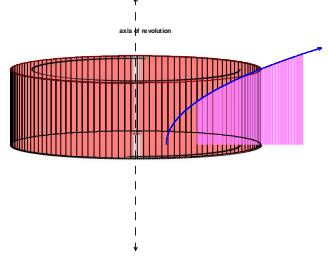
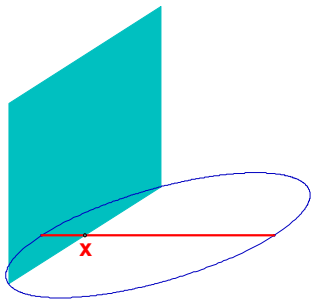
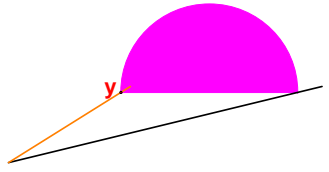


Topic	Equation	Graphic	Word Problems	Approximation	Algebraic										
<p>Definite Integral from a to b</p>	$\int_a^b f(x)dx$	<p>Signed area between f and x-axis on $[a,b]$.</p> 	<p>Accumulation of values of f on $[a,b]$</p> 	<p>Riemann Sum on $[a,b]$ (Not always equal length subintervals)</p> <table border="1" data-bbox="1339 391 1675 464"> <tr> <td>x</td> <td>2</td> <td>5</td> <td>7</td> <td>8</td> </tr> <tr> <td>$f(x)$</td> <td>10</td> <td>30</td> <td>40</td> <td>20</td> </tr> </table> <p>$(5-2)(10) + (7-5)(30) + (8-7)(40)$ = Left Riemann Sum</p>	x	2	5	7	8	$f(x)$	10	30	40	20	<p>$F(b)-F(a)$ where $F'(x)=f(x)$ <u>Fundamental Theorem of Calculus</u> $F(b)-F(a)=\int_a^b f(x)dx$ $F(b)=\int_a^b f(x)dx+F(a)$ $f(b)=\int_a^b f'(x)dx+f(a)$</p>
x	2	5	7	8											
$f(x)$	10	30	40	20											
<p>Average Value for f</p>	$\frac{1}{b-a} \int_a^b f(x)dx$	<p>There is a $c \in [a,b]$ such that $\int_a^b f(x)dx = f(c)[b-a]$</p>  <p>There is some rectangle whose height is on the graph with area equal to the integral.</p>	<p>The average value of f on $[a,b]$ is $Avg(f) = \frac{1}{b-a} \int_a^b f(x)dx$</p>  <p>Find average value of $f(x) = (x-2)^2$ on $[0,3]$</p>	<p>Average value of f is approximately the Riemann Sum of f on $[a, b]$ divided by $b-a$</p> <table border="1" data-bbox="1339 885 1675 958"> <tr> <td>x</td> <td>2</td> <td>5</td> <td>7</td> <td>8</td> </tr> <tr> <td>$f(x)$</td> <td>10</td> <td>30</td> <td>40</td> <td>20</td> </tr> </table> <p>Use Right Riemann Sum to estimate average value of f.</p> $\frac{1}{8-2} [(5-2)(30) + (7-5)(40) + (8-7)(20)]$ $= \frac{1}{6} [90 + 80 + 20]$ $= \frac{1}{6} (210)$ $= 35$	x	2	5	7	8	$f(x)$	10	30	40	20	<p>Mean Value Theorem for Integrals</p> $\frac{1}{b-a} \int_a^b f(x)dx = f(c)$ <p>where $c \in [a,b]$</p>
x	2	5	7	8											
$f(x)$	10	30	40	20											

Topic	Equation	Graphic	Word Problems	Approximation	Algebraic																				
Derivative	$f'(x) = \frac{df}{dx}$	 <p>The slope of the tangent line to f</p>	<p>Instantaneous Rate of Change: <u>Example:</u> Instantaneous velocity = $p'(t)$ where $p(t)$ is position function</p>	<table border="1" data-bbox="1339 332 1675 402"> <tr> <td>x</td> <td>2</td> <td>5</td> <td>7</td> <td>8</td> </tr> <tr> <td>$f(x)$</td> <td>10</td> <td>30</td> <td>40</td> <td>20</td> </tr> </table> $f'(6) \approx \frac{40 - 30}{7 - 5} = 5$	x	2	5	7	8	$f(x)$	10	30	40	20	<p>The limit of the rate change of f.</p> $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$										
x	2	5	7	8																					
$f(x)$	10	30	40	20																					
Relative Extrema	$f'(x)$ changes sign	 <p>At this point, f' changes from positive to negative</p> <p>At this point, f' changes from negative to positive</p>	<ul style="list-style-type: none"> • The rate of change changes sign • The particle changes direction • The values change from increasing to decreasing or vice-versa • The particle stops momentarily • The velocity is momentarily zero 	<table border="1" data-bbox="1354 633 1659 966"> <thead> <tr> <th>t (hours)</th> <th>$R(t)$ (gallons per hour)</th> </tr> </thead> <tbody> <tr><td>0</td><td>9.6</td></tr> <tr><td>3</td><td>10.4</td></tr> <tr><td>6</td><td>10.8</td></tr> <tr><td>9</td><td>11.2</td></tr> <tr><td>12</td><td>11.4</td></tr> <tr><td>15</td><td>11.3</td></tr> <tr><td>18</td><td>10.7</td></tr> <tr><td>21</td><td>10.2</td></tr> <tr><td>24</td><td>9.6</td></tr> </tbody> </table> <p>By MVT, $\frac{11.4 - 9.6}{12 - 0} = .15$ $c \in (0, 12)$ so there is a c such that $R'(c) = .15$ Similarly, there is a $d \in (12, 24)$ such that $R'(d) = -0.15$</p>	t (hours)	$R(t)$ (gallons per hour)	0	9.6	3	10.4	6	10.8	9	11.2	12	11.4	15	11.3	18	10.7	21	10.2	24	9.6	<p><u>Relative max</u> $f(a) \geq f(x)$ for all x in some interval</p> <p><u>Relative Min</u> $f(a) \leq f(x)$ for all x in some interval</p>
t (hours)	$R(t)$ (gallons per hour)																								
0	9.6																								
3	10.4																								
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15	11.3																								
18	10.7																								
21	10.2																								
24	9.6																								

Topic	Equation	Graphic	Word Problems	Approximation	Tangent Lines																				
Concavity	$f''(x) > 0$ concave up $f''(x) < 0$ concave down	concave up: tangent line is below curve 	<u>Concave Up:</u> <ul style="list-style-type: none"> the rate of change is increasing (more positive) acceleration > 0 $v(t) < 0$: particle is slowing down $v(t) > 0$: particle is speeding up <u>Concave Down:</u> <ul style="list-style-type: none"> the rate of change is decreasing (more negative) acceleration < 0 $v(t) < 0$: particle is speeding up $v(t) > 0$: particle is slowing down 	<table border="1" data-bbox="1339 300 1675 373"> <tr> <td>x</td> <td>2</td> <td>5</td> <td>7</td> <td>8</td> </tr> <tr> <td>$f(x)$</td> <td>10</td> <td>30</td> <td>40</td> <td>20</td> </tr> </table> $\frac{30-10}{5-2} = 6.667$ $\frac{40-30}{7-5} = 5$ $\frac{20-40}{8-7} = -20$ <p>Concave down because the derivative is decreasing.</p>	x	2	5	7	8	$f(x)$	10	30	40	20	Concave up: The tangent line approximations are under approximations Concave down: The tangent line approximations are over approximations										
x	2	5	7	8																					
$f(x)$	10	30	40	20																					
Inflection Points	$f''(x)$ changes sign		Rate of Change goes from increasing to decreasing or vice versa. Velocity of particle changes from speeding up to slowing down or vice versa.	<table border="1" data-bbox="1354 901 1659 1185"> <thead> <tr> <th>t (hours)</th> <th>$R(t)$ (gallons per hour)</th> </tr> </thead> <tbody> <tr><td>0</td><td>9.6</td></tr> <tr><td>3</td><td>10.4</td></tr> <tr><td>6</td><td>10.8</td></tr> <tr><td>9</td><td>11.2</td></tr> <tr><td>12</td><td>11.4</td></tr> <tr><td>15</td><td>11.3</td></tr> <tr><td>18</td><td>10.7</td></tr> <tr><td>21</td><td>10.2</td></tr> <tr><td>24</td><td>9.6</td></tr> </tbody> </table> <p>If $G(t)$ is the number of gallons that has flowed through the pipe from time = 0 to time = t then $G''(t) = 0$ for t between 0 and 24 hours.</p>	t (hours)	$R(t)$ (gallons per hour)	0	9.6	3	10.4	6	10.8	9	11.2	12	11.4	15	11.3	18	10.7	21	10.2	24	9.6	The tangent line crosses the graph of the curve at an inflection point.
t (hours)	$R(t)$ (gallons per hour)																								
0	9.6																								
3	10.4																								
6	10.8																								
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21	10.2																								
24	9.6																								

Volume	Horizontal Axis	Vertical Axis	Cross-Sections Perpendicular to x axis	Cross-Sections Perpendicular to y axis
<p>Volume = $\int_{x=a}^{x=b} A(x)dx$</p> <p>Volume = $\int_{y=c}^{y=d} A(y)dy$</p>	 <p>Volume = $\pi \int_a^b (R(x)^2 - r(x)^2) dx$</p> <p>$R(x) = f(x) - axis$ $r(x) = g(x) - axis$</p> <p><i>f(x) is furthest from axis</i> <i>g(x) is closest to axis</i></p>	 <p>Volume = $\int_a^b 2\pi(\text{height})(\text{radius})dx$</p> <p>height = $f(x) - g(x)$ where <i>f</i> is furthest from x-axis, and <i>g(x)</i> is closer to x-axis. radius = $(x - axis)$</p>	 <p>Volume = $\int_a^b A(x)dx$</p> <p>Where $A(x)$ is the area of the cross-section as a function of x.</p>	 <p>Volume = $\int_c^d A(y)dy$</p> <p>Where $A(y)$ is the area of the cross-section as a function of y.</p>